

# Mathematics

(www.tiwariacademy.com: Focus on free education)  
(Chapter – 3) (Linear equations in two variables)

(Class – X)

## Exercise 3.6

### Question 1:

Solve the following pairs of equations by reducing them to a pair of linear equations:

$$(i) \quad \frac{1}{2x} + \frac{1}{3y} = 2$$
$$\frac{1}{3x} + \frac{1}{2y} = \frac{13}{6}$$

$$(ii) \quad \frac{2}{\sqrt{x}} + \frac{3}{\sqrt{y}} = 2$$
$$\frac{4}{\sqrt{x}} - \frac{9}{\sqrt{y}} = -1$$

$$(iii) \quad \frac{4}{x} + 3y = 14$$
$$\frac{3}{x} - 4y = 23$$

$$(iv) \quad \frac{5}{x-1} + \frac{1}{y-2} = 2$$
$$\frac{6}{x-1} - \frac{3}{y-2} = 1$$

$$(v) \quad \frac{7x-2y}{xy} = 5$$
$$\frac{8x+7y}{xy} = 15$$

$$(vi) \quad 6x+3y = 6xy$$
$$2x+4y = 5xy$$

$$(vii) \quad \frac{10}{x+y} + \frac{2}{x-y} = 4$$
$$\frac{15}{x+y} - \frac{5}{x-y} = -2$$

$$(viii) \quad \frac{1}{3x+y} + \frac{1}{3x-y} = \frac{3}{4}$$
$$\frac{1}{2(3x+y)} - \frac{1}{2(3x-y)} = \frac{-1}{8}$$

### Answer 1:

$$(i) \quad \frac{1}{2x} + \frac{1}{3y} = 2$$
$$\frac{1}{3x} + \frac{1}{2y} = \frac{13}{6}$$

Let  $\frac{1}{x} = p$  and  $\frac{1}{y} = q$ , then the equations change as follows.

$$\frac{p}{2} + \frac{q}{3} = 2 \quad \Rightarrow \quad 3p + 2q - 12 = 0 \quad (1)$$

$$\frac{p}{3} + \frac{q}{2} = \frac{13}{6} \quad \Rightarrow \quad 2p + 3q - 13 = 0 \quad (2)$$

Using cross-multiplication method, we obtain

# Mathematics

(www.tiwariacademy.com: Focus on free education)  
(Chapter – 3) (Linear equations in two variables)

(Class – X)

$$\frac{p}{-26 - (-36)} = \frac{q}{-24 - (-39)} = \frac{1}{9 - 4}$$

$$\frac{p}{10} = \frac{q}{15} = \frac{1}{5}$$

$$\frac{p}{10} = \frac{1}{5} \text{ and } \frac{q}{15} = \frac{1}{5}$$

$$p = 2 \text{ and } q = 3$$

$$\frac{1}{x} = 2 \text{ and } \frac{1}{y} = 3$$

$$x = \frac{1}{2} \text{ and } y = \frac{1}{3}$$

$$(ii) \quad \frac{2}{\sqrt{x}} + \frac{3}{\sqrt{y}} = 2$$

$$\frac{4}{\sqrt{x}} - \frac{9}{\sqrt{y}} = -1$$

Putting  $\frac{1}{\sqrt{x}} = p$  and  $\frac{1}{\sqrt{y}} = q$  in the given equations, we obtain

$$2p + 3q = 2 \quad (1)$$

$$4p - 9q = -1 \quad (2)$$

Multiplying equation (1) by 3, we obtain

$$6p + 9q = 6 \quad (3)$$

Adding equation (2) and (3), we obtain

$$10p = 5$$

$$p = \frac{1}{2} \quad (4)$$

Putting in equation (1), we obtain

$$2 \times \frac{1}{2} + 3q = 2$$

$$3q = 1$$

$$q = \frac{1}{3}$$

# Mathematics

([www.tiwariacademy.com](http://www.tiwariacademy.com): Focus on free education)  
(Chapter – 3) (Linear equations in two variables)

(Class – X)

$$p = \frac{1}{\sqrt{x}} = \frac{1}{2}$$

$$\sqrt{x} = 2$$

$$x = 4$$

$$\text{and } q = \frac{1}{\sqrt{y}} = \frac{1}{3}$$

$$\sqrt{y} = 3$$

$$y = 9$$

Hence,  $x = 4, y = 9$

$$\begin{aligned} \text{(iii)} \quad \frac{4}{x} + 3y &= 14 \\ \frac{3}{x} - 4y &= 23 \end{aligned}$$

Substituting  $\frac{1}{x} = p$  in the given equations, we obtain

$$4p + 3y = 14 \quad \Rightarrow \quad 4p + 3y - 14 = 0 \quad (1)$$

$$3p - 4y = 23 \quad \Rightarrow \quad 3p - 4y - 23 = 0 \quad (2)$$

By cross-multiplication, we obtain

$$\frac{p}{-69 - 56} = \frac{y}{-42 - (-92)} = \frac{1}{-16 - 9}$$

$$\frac{p}{-125} = \frac{y}{50} = \frac{-1}{25}$$

$$\frac{p}{-125} = \frac{-1}{25} \quad \text{and} \quad \frac{y}{50} = \frac{-1}{25}$$

$$p = 5 \quad \text{and} \quad y = -2$$

$$p = \frac{1}{x} = 5$$

$$x = \frac{1}{5}$$

$$y = -2$$

# Mathematics

([www.tiwariacademy.com](http://www.tiwariacademy.com): Focus on free education)  
(Chapter – 3) (Linear equations in two variables)  
(Class – X)

$$\begin{aligned} \text{(iv)} \quad \frac{5}{x-1} + \frac{1}{y-2} &= 2 \\ \frac{6}{x-1} - \frac{3}{y-2} &= 1 \end{aligned}$$

Putting  $\frac{1}{x-1} = p$  and  $\frac{1}{y-2} = q$  in the given equation, we obtain

$$5p + q = 2 \quad (1)$$

$$6p - 3q = 1 \quad (2)$$

Multiplying equation (1) by 3, we obtain

$$15p + 3q = 6 \quad (3)$$

Adding (2) and (3), we obtain

$$21p = 7$$

$$p = \frac{1}{3}$$

Putting this value in equation (1), we obtain

$$5 \times \frac{1}{3} + q = 2$$

$$q = 2 - \frac{5}{3} = \frac{1}{3}$$

$$p = \frac{1}{x-1} = \frac{1}{3}$$

$$\Rightarrow x - 1 = 3$$

$$\Rightarrow x = 4$$

$$q = \frac{1}{y-2} = \frac{1}{3}$$

$$y - 2 = 3$$

$$y = 5$$

$$\therefore x = 4, y = 5$$

# Mathematics

([www.tiwariacademy.com](http://www.tiwariacademy.com): Focus on free education)  
(Chapter – 3) (Linear equations in two variables)

(Class – X)

$$\begin{aligned} \text{(v)} \quad \frac{7x-2y}{xy} &= 5 \\ \frac{7}{y} - \frac{2}{x} &= 5 \quad (1) \\ \frac{8x+7y}{xy} &= 15 \\ \frac{8}{y} + \frac{7}{x} &= 15 \quad (2) \end{aligned}$$

Putting  $\frac{1}{x} = p$  and  $\frac{1}{y} = q$  in the given equation, we obtain

$$-2p + 7q = 5 \quad \Rightarrow \quad -2p + 7q - 5 = 0 \quad (3)$$

$$7p + 8q = 15 \quad \Rightarrow \quad 7p + 8q - 15 = 0 \quad (4)$$

By cross-multiplication method, we obtain

$$\frac{p}{-105 - (-40)} = \frac{q}{-35 - 30} = \frac{1}{-16 - 49}$$

$$\frac{p}{-65} = \frac{q}{-65} = \frac{1}{-65}$$

$$\frac{p}{-65} = \frac{1}{-65} \quad \text{and} \quad \frac{q}{-65} = \frac{1}{-65}$$

$$p = 1 \quad \text{and} \quad q = 1$$

$$p = \frac{1}{x} = 1 \quad q = \frac{1}{y} = 1$$

$$x = 1 \quad y = 1$$

$$\begin{aligned} \text{(vi)} \quad 6x + 3y &= 6xy \\ \Rightarrow \frac{6}{y} + \frac{3}{x} &= 6 \quad (1) \\ 2x + 4y &= 5xy \\ \frac{2}{y} + \frac{4}{x} &= 5 \quad (2) \end{aligned}$$

# Mathematics

([www.tiwariacademy.com](http://www.tiwariacademy.com): Focus on free education)  
(Chapter – 3) (Linear equations in two variables)

(Class – X)

Putting  $\frac{1}{x} = p$  and  $\frac{1}{y} = q$   
 $3p + 6q - 6 = 0$   
 $4p + 2q - 5 = 0$

By cross-multiplication method, we obtain

$$\frac{p}{-30 - (-12)} = \frac{q}{-24 - (-15)} = \frac{1}{6 - 24}$$

$$\frac{p}{-18} = \frac{q}{-9} = \frac{1}{-18}$$

$$\frac{p}{-18} = \frac{1}{-18} \text{ and } \frac{q}{-9} = \frac{1}{-18}$$

$$p = 1 \text{ and } q = \frac{1}{2}$$

$$p = \frac{1}{x} = 1 \quad q = \frac{1}{y} = \frac{1}{2}$$

$$x = 1 \quad y = 2$$

Hence,  $x = 1, y = 2$

(vii)  $\frac{10}{x+y} + \frac{2}{x-y} = 4$   
 $\frac{15}{x+y} - \frac{5}{x-y} = -2$

Putting  $\frac{1}{x+y} = p$  and  $\frac{1}{x-y} = q$  in the given equations, we obtain

$$10p + 2q = 4 \quad \Rightarrow \quad 10p + 2q - 4 = 0 \quad (1)$$

$$15p - 5q = -2 \quad \Rightarrow \quad 15p - 5q + 2 = 0 \quad (2)$$

Using cross-multiplication method, we obtain

# Mathematics

(www.tiwariacademy.com: Focus on free education)  
(Chapter – 3) (Linear equations in two variables)

(Class – X)

$$\frac{p}{4-20} = \frac{q}{-60-(20)} = \frac{1}{-50-30}$$

$$\frac{p}{-16} = \frac{q}{-80} = \frac{1}{-80}$$

$$\frac{p}{-16} = \frac{1}{-80} \text{ and } \frac{q}{-80} = \frac{1}{-80}$$

$$p = \frac{1}{5} \text{ and } q = 1$$

$$p = \frac{1}{x+y} = \frac{1}{5} \text{ and } q = \frac{1}{x-y} = 1$$

$$x+y=5 \quad (3)$$

$$\text{and } x-y=1 \quad (4)$$

Adding equation (3) and (4), we obtain

$$2x=6$$

$$x=3 \quad (5)$$

Substituting in equation (3), we obtain y

$$= 2$$

Hence,  $x = 3$ ,  $y = 2$

$$(viii) \quad \frac{1}{3x+y} + \frac{1}{3x-y} = \frac{3}{4}$$

$$\frac{1}{2(3x+y)} - \frac{1}{2(3x-y)} = \frac{-1}{8}$$

Putting  $\frac{1}{3x+y} = p$  and  $\frac{1}{3x-y} = q$

in these equations,

$$p+q = \frac{3}{4} \quad (1)$$

$$\frac{p}{2} - \frac{q}{2} = \frac{-1}{8}$$

$$p-q = \frac{-1}{4} \quad (2)$$

Adding (1) and (2), we obtain

# Mathematics

([www.tiwariacademy.com](http://www.tiwariacademy.com): Focus on free education)  
(Chapter – 3) (Linear equations in two variables)

(Class – X)

$$2p = \frac{3}{4} - \frac{1}{4}$$

$$2p = \frac{1}{2}$$

$$p = \frac{1}{4}$$

Substituting in (2), we obtain

$$\frac{1}{4} - q = \frac{-1}{4}$$

$$q = \frac{1}{4} + \frac{1}{4} = \frac{1}{2}$$

$$p = \frac{1}{3x+y} = \frac{1}{4}$$

$$3x + y = 4 \quad (3)$$

$$q = \frac{1}{3x-y} = \frac{1}{2}$$

$$3x - y = 2 \quad (4)$$

Adding equations (3) and (4), we obtain

$$6x = 6$$

$$x = 1 \quad (5)$$

Substituting in (3), we obtain

$$3(1) + y = 4$$

$$y = 1$$

Hence,  $x = 1$ ,  $y = 1$

## Question 2:

Formulate the following problems as a pair of equations, and hence find their solutions:

- (i) Ritu can row downstream 20 km in 2 hours, and upstream 4 km in 2 hours. Find her speed of rowing in still water and the speed of the current.
- (ii) 2 women and 5 men can together finish an embroidery work in 4 days, while 3 women and 6 men can finish it in 3 days. Find the time taken by 1 woman alone to finish the work, and also that taken by 1 man alone.
- (iii) Roohi travels 300 km to her home partly by train and partly by bus. She takes 4 hours if she travels 60 km by train and remaining by bus. If she travels 100 km by train and the remaining by bus, she takes 10 minutes longer. Find the speed of the train and the bus separately.



# Mathematics

(www.tiwariacademy.com: Focus on free education)  
(Chapter – 3) (Linear equations in two variables)

(Class – X)

## Answer 2:

(i) Let the speed of Ritu in still water and the speed of stream be  $x$  km/h and  $y$  km/h respectively.

Speed of Ritu while rowing

Upstream =  $x - y$  km/h

Downstream =  $x + y$  km/h

According to question,

$$2(x+y) = 20$$

$$\Rightarrow x+y = 10 \quad (1)$$

$$2(x-y) = 4$$

$$\Rightarrow x-y = 2 \quad (2)$$

Adding equation (1) and (2), we obtain

$$2x = 12 \Rightarrow x = 6$$

Putting this in equation (1), we obtain  $y = 4$

Hence, Ritu's speed in still water is 6 km/h and the speed of the current is 4 km/h.

(ii) Let the number of days taken by a woman and a man be  $x$  and  $y$  respectively.

Therefore, work done by a woman in 1 day =  $1/x$

Work done by a man in 1 day =  $1/y$

According to the question,

$$4\left(\frac{2}{x} + \frac{5}{y}\right) = 1$$

$$\frac{2}{x} + \frac{5}{y} = \frac{1}{4}$$

$$3\left(\frac{3}{x} + \frac{6}{y}\right) = 1$$

$$\frac{3}{x} + \frac{6}{y} = \frac{1}{3}$$

Putting  $\frac{1}{x} = p$  and  $\frac{1}{y} = q$

$$2p + 5q = \frac{1}{4}$$

$$\Rightarrow 8p + 20q = 1$$

$$3p + 6q = \frac{1}{3}$$

$$\Rightarrow 9p + 18q = 1$$



# Mathematics

([www.tiwariacademy.com](http://www.tiwariacademy.com): Focus on free education)  
(Chapter – 3) (Linear equations in two variables)

(Class – X)

By cross-multiplication, we obtain

$$\frac{p}{-20 - (-18)} = \frac{q}{-9 - (-8)} = \frac{1}{144 - 180}$$

$$\frac{p}{-2} = \frac{q}{-1} = \frac{1}{-36}$$

$$\frac{p}{-2} = \frac{-1}{36} \text{ and } \frac{q}{-1} = \frac{1}{-36}$$

$$p = \frac{1}{18} \text{ and } q = \frac{1}{36}$$

$$p = \frac{1}{x} = \frac{1}{18} \text{ and } q = \frac{1}{y} = \frac{1}{36}$$

$$x = 18 \quad y = 36$$

Hence, number of days taken by a woman = 18

Number of days taken by a man = 36

(iii) Let the speed of train and bus be  $u$  km/h and  $v$  km/h respectively.

According to the given information,

$$\frac{60}{u} + \frac{240}{v} = 4 \quad (1)$$

$$\frac{100}{u} + \frac{200}{v} = \frac{25}{6} \quad (2)$$

Putting  $\frac{1}{u} = p$  and  $\frac{1}{v} = q$  in these equations, we obtain

$$60p + 240q = 4 \quad (3)$$

$$100p + 200q = \frac{25}{6}$$

$$600p + 1200q = 25 \quad (4)$$

Multiplying equation (3) by 10, we obtain

$$600p + 2400q = 40 \quad (5)$$

Subtracting equation (4) from (5), we obtain

$$1200q = 15$$

$$q = \frac{15}{1200} = \frac{1}{80} \quad (6)$$

Substituting in equation (3), we obtain

# Mathematics

([www.tiwariacademy.com](http://www.tiwariacademy.com): Focus on free education)  
(Chapter – 3) (Linear equations in two variables)

(Class – X)

$$60p + 3 = 4$$

$$60p = 1$$

$$p = \frac{1}{60}$$

$$p = \frac{1}{u} = \frac{1}{60} \quad \text{and} \quad q = \frac{1}{v} = \frac{1}{80}$$

$$u = 60 \text{ km/h} \quad \text{and} \quad v = 80 \text{ km/h}$$

Hence, speed of train = 60 km/h

Speed of bus = 80 km/h