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(Chapter – 14) (Mathematical Reasoning)
(Class – XI)

Miscellaneous Exercise on Chapter 14

Question 1:

Write the negation of the following statements:

- (i) p: For every positive real number x, the number x 1 is also positive.
- (ii) q: All cats scratch.
- (iii) r. For every real number x, either x > 1 or x < 1.
- (iv) s: There exists a number x such that 0 < x < 1.

Answer 1:

(i) The negation of statement p is as follows.

There exists a positive real number x, such that x - 1 is not positive.

(ii) The negation of statement q is as follows.

There exists a cat that does not scratch.

(iii) The negation of statement r is as follows.

There exists a real number x, such that neither x > 1 nor x < 1.

(iv) The negation of statement s is as follows. There does not exist a number x, such that 0 < x < 1.

Question 2:

State the converse and contrapositive of each of the following statements:

- (i) p: A positive integer is prime only if it has no divisors other than 1 and itself.
- (ii) q: I go to a beach whenever it is a sunny day.
- (iii) r. If it is hot outside, then you feel thirsty.

Answer 2:

(i) Statement *p* can be written as follows.

If a positive integer is prime, then it has no divisors other than 1 and itself.

The converse of the statement is as follows.

If a positive integer has no divisors other than 1 and itself, then it is prime.

The contrapositive of the statement is as follows.



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If positive integer has divisors other than 1 and itself, then it is not prime.

(ii) The given statement can be written as follows.

If it is a sunny day, then I go to a beach.

The converse of the statement is as follows.

If I go to a beach, then it is a sunny day.

The contrapositive of the statement is as follows.

If I do not go to a beach, then it is not a sunny day.

(iii) The converse of statement r is as follows.

If you feel thirsty, then it is hot outside.

The contrapositive of statement *r* is as follows. If you do not feel thirsty, then it is not hot outside.

Question 3:

Write each of the statements in the form "if p, then q".

- (i) *p*: It is necessary to have a password to log on to the server.
- (ii) q: There is traffic jam whenever it rains.
- (iii) r. You can access the website only if you pay a subscription fee.

Answer 3:

(i) Statement *p* can be written as follows.

If you log on to the server, then you have a password.

(ii) Statement *q* can be written as follows.

If it rains, then there is a traffic jam.

(iii) Statement *r* can be written as follows. If you can access the website, then you pay a subscription fee.

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Question 4:

Re write each of the following statements in the form "p if and only if q".

- (i) *p*: If you watch television, then your mind is free and if your mind is free, then you watch television.
- (ii) q: For you to get an A grade, it is necessary and sufficient that you do all the homework regularly.
- (iii) r. If a quadrilateral is equiangular, then it is a rectangle and if a quadrilateral is a rectangle, then it is equiangular.

Answer 4:

- (i) You watch television if and only if your mind is free.
- (ii) You get an A grade if and only if you do all the homework regularly.(iii) A quadrilateral is equiangular if and only if it is a rectangle.

Question 5:

Given below are two statements *p*: 25 is a multiple of 5. *q*: 25 is a multiple of 8. Write the compound statements connecting these two statements with "And" and "Or". In both cases check the validity of the compound statement.

Answer 5:

The compound statement with 'And' is "25 is a multiple of 5 and 8".

This is a false statement, since 25 is not a multiple of 8.

The compound statement with 'Or' is "25 is a multiple of 5 or 8". This is a true statement, since 25 is not a multiple of 8 but it is a multiple of 5.

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Question 6:

Check the validity of the statements given below by the method given against it.

- (i) p: The sum of an irrational number and a rational number is irrational (by contradiction method).
- (ii) q: If n is a real number with n > 3, then $n^2 > 9$ (by contradiction method).

Answer 6:

(i) The given statement is as follows.

p: the sum of an irrational number and a rational number is irrational.

Let us assume that the given statement, *p*, is false. That is, we assume that the sum of an irrational number and a rational number is rational.

Therefore $\sqrt{a} + \frac{b}{c} = \frac{d}{e}$, where \sqrt{a} is irrational and b, c, d, e are integers.

 $\frac{d}{e} - \frac{b}{c}$ is a rational number and \sqrt{a} is an irrational number.

This is a contradiction. Therefore, our assumption is wrong.

Therefore, the sum of an irrational number and a rational number is rational.

Thus, the given statement is true.

(ii) The given statement, q, is as follows.

If *n* is a real number with n > 3, then $n^2 > 9$.

Let us assume that n is a real number with n > 3, but $n^2 > 9$ is not true.

That is, $n^2 < 9$

Then, n > 3 and n is a real number.

Squaring both the sides, we obtain $n^2 > (3)^2$

 $\Rightarrow n^2 > 9$, which is a contradiction, since we have assumed that $n^2 < 9$.

Thus, the given statement is true. That is, if n is a real number with n > 3, then $n^2 > 9$.

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Question 7:

Write the following statement in five different ways, conveying the same meaning. *p: If triangle is equiangular, then it is an obtuse angled triangle.*

Answer 7:

The given statement can be written in five different ways as follows.

- (i) A triangle is equiangular implies that it is an obtuse-angled triangle.
- (ii) A triangle is equiangular only if it is an obtuse-angled triangle.
- (iii) For a triangle to be equiangular, it is necessary that the triangle is an obtuse-angled triangle.
- (iv) For a triangle to be an obtuse-angled triangle, it is sufficient that the triangle is equiangular.
- (v) If a triangle is not an obtuse-angled triangle, then the triangle is not equiangular.