

Mathematics

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(Chapter – 16) (Probability)

(Class – XI)

Exercise 16.2

Question 1:

A die is rolled. Let E be the event “die shows 4” and F be the event “die shows even number”.

Are E and F mutually exclusive?

Answer 1:

When a die is rolled, the sample space is given by

$$S = \{1, 2, 3, 4, 5, 6\}$$

Accordingly, $E = \{4\}$ and $F = \{2, 4, 6\}$

It is observed that $E \cap F = \{4\} \neq \emptyset$ Therefore, E and F are not mutually exclusive events.

Question 2:

A die is thrown. Describe the following events:

(i) A: a number less than 7

(ii) B: a number greater than 7

(iii) C: a multiple of 3

(iv) D: a number less than 4

(v) E: an even number greater than 4

(vi) F: a number not less than 3

Also find $A \cup B, A \cap B, B \cup C, E \cap F, D \cap E, A - C, D - E, E \cap F', F'$

Answer 2:

When a die is thrown, the sample space is given by $S = \{1, 2, 3, 4, 5, 6\}$. Accordingly:

(i) $A = \{1, 2, 3, 4, 5, 6\}$

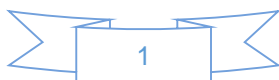
(ii) $B = \emptyset$

(iii) $C = \{3, 6\}$

(iv) $D = \{1, 2, 3\}$

(v) $E = \{6\}$

(vi) $F = \{3, 4, 5, 6\}$



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$$A \cup B = \{1, 2, 3, 4, 5, 6\}, A \cap B = \Phi$$

$$A \cup C = \{3, 6\}, E \cap F = \{6\}$$

$$D \cap E = \Phi, A - C = \{1, 2, 4, 5\}$$

$$D - E = \{1, 2, 3\},$$

$$F' = \{1, 2\}$$

$$E \cap F' = \Phi$$

Question 3:

An experiment involves rolling a pair of dice and recording the numbers that come up. Describe the following events:

A: the sum is greater than 8,

B: 2 occurs on either die

C: The sum is at least 7 and a multiple of 3.

Which pairs of these events are mutually exclusive?

Answer 3:

When a pair of dice is rolled, the sample space is given by

$$S = \{(x, y) : x, y = 1, 2, 3, 4, 5, 6\}$$
$$= \left\{ \begin{array}{l} (1,1), (1,2), (1,3), (1,4), (1,5), (1,6) \\ (2,1), (2,2), (2,3), (2,4), (2,5), (2,6) \\ (3,1), (3,2), (3,3), (3,4), (3,5), (3,6) \\ (4,1), (4,2), (4,3), (4,4), (4,5), (4,6) \\ (5,1), (5,2), (5,3), (5,4), (5,5), (5,6) \\ (6,1), (6,2), (6,3), (6,4), (6,5), (6,6) \end{array} \right\}$$

Accordingly,

$$A = \{(3,6), (4,5), (4,6), (5,4), (5,5), (5,6), (6,3), (6,4), (6,5), (6,6)\}$$

$$B = \{(2,1), (2,2), (2,3), (2,4), (2,5), (2,6), (1,2), (3,2), (4,2), (5,2), (6,2)\}$$

$$C = \{(3,6), (4,5), (5,4), (6,3), (6,6)\}$$



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It is observed that

$$A \cap B = \Phi$$

$$B \cap C = \Phi$$

$$C \cap A = \{(3,6), (4,5), (5,4), (6,3), (6,6)\} \neq \phi$$

Hence, events A and B and events B and C are mutually exclusive.

Question 4:

Three coins are tossed once. Let A denote the event ‘three heads show’, B denote the event ‘two heads and one tail show’. C denote the event ‘three tails show’ and D denote the event ‘a head shows on the first coin’. Which events are

(i) mutually exclusive?

(ii) simple?

(iii) compound?

Answer 4:

When three coins are tossed, the sample space is given by

$$S = \{HHH, HHT, HTH, HTT, THH, THT, TTH, TTT\}$$

Accordingly,

$$A = \{HHH\}$$

$$B = \{HHT, HTH, THH\}$$

$$C = \{TTT\}$$

$$D = \{HHH, HHT, HTH, HTT\}$$

We now observe that

$$A \cap B = \Phi, A \cap C = \Phi, A \cap D = \{HHH\} \neq \Phi$$

$$B \cap C = \Phi, B \cap D = \{HHT, \{HTH\} \neq \Phi$$

$$C \cap D = \Phi$$

(i) Event A and B; event A and C; event B and C; and event C and D are all mutually exclusive.



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(ii) If an event has only one sample point of a sample space, it is called a simple event.
Thus, A and C are simple events.

(iii) If an event has more than one sample point of a sample space, it is called a compound event.

Thus, B and D are compound events.

Question 5:

Three coins are tossed. Describe

- (i) Two events which are mutually exclusive.
- (ii) Three events which are mutually exclusive and exhaustive.
- (iii) Two events, which are not mutually exclusive.
- (iv) Two events which are mutually exclusive but not exhaustive.
- (v) Three events which are mutually exclusive but not exhaustive.

Answer 5:

When three coins are tossed, the sample space is given by

$S = \{HHH, HHT, HTH, HTT, THH, THT, TTH, TTT\}$

(i) Two events that are mutually exclusive can be

A: getting no heads and

B: getting no tails

This is because sets

$A = \{TTT\}$ and $B = \{HHH\}$ are disjoint.

(ii) Three events that are mutually exclusive and exhaustive can be

A: getting no heads

B: getting exactly one head

C: getting at least two heads

i.e.,

$A = \{TTT\}$



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$$B = \{HTT, THT, TTH\}$$

$$C = \{HHH, HHT, HTH, THH\}$$

This is because $A \cap B = B \cap C = C \cap A = \Phi$ and $A \cup B \cup C = S$

(iii) Two events that are not mutually exclusive can be

A: getting three heads

B: getting at least 2 heads

i.e.,

$$A = \{HHH\}$$

$$B = \{HHH, HHT, HTH, THH\}$$

This is because $A \cap B = \{HHH\} \neq \Phi$

(iv) Two events which are mutually exclusive but not exhaustive can be

A: getting exactly one head

B: getting exactly one tail That is

$$A = \{HTT, THT, TTH\}$$

$$B = \{HHT, HTH, THH\}$$

It is because, $A \cap B = \Phi$, but $A \cup B \neq S$

(v) Three events that are mutually exclusive but not exhaustive can be

A: getting exactly three heads

B: getting one head and two tails

C: getting one tail and two heads

i.e.,

$$A = \{HHH\}$$

$$B = \{HTT, THT, TTH\}$$

$$C = \{HHT, HTH, THH\}$$

This is because $A \cap B = B \cap C = C \cap A = \Phi$, but $A \cup B \cup C \neq S$



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Question 6:

Two dice are thrown. The events A, B and C are as follows:

A: getting an even number on the first die.

B: getting an odd number on the first die.

C: getting the sum of the numbers on the dice ≤ 5

Describe the events

(i) A'

(ii) not B

(iii) A or B

(iv) A and B

(v) A but not C

(vi) B or C

(vii) B and C

(viii) $A \cap B' \cap C'$

Answer 6:

When two dice are thrown, the sample space is given by

$$S = \{(x, y) : x, y = 1, 2, 3, 4, 5, 6\}$$

$$= \left\{ \begin{array}{l} (1,1), (1,2), (1,3), (1,4), (1,5), (1,6) \\ (2,1), (2,2), (2,3), (2,4), (2,5), (2,6) \\ (3,1), (3,2), (3,3), (3,4), (3,5), (3,6) \\ (4,1), (4,2), (4,3), (4,4), (4,5), (4,6) \\ (5,1), (5,2), (5,3), (5,4), (5,5), (5,6) \\ (6,1), (6,2), (6,3), (6,4), (6,5), (6,6) \end{array} \right\}$$

Accordingly,

$$A = \left\{ (2,1), (2,2), (2,3), (2,4), (2,5), (2,6), (4,1), (4,2), (4,3), \right. \\ \left. (4,4), (4,5), (4,6), (6,1), (6,2), (6,3), (6,4), (6,5), (6,6) \right\}$$

$$B = \left\{ (1,1), (1,2), (1,3), (1,4), (1,5), (1,6), (3,1), (3,2), (3,3), \right. \\ \left. (3,4), (3,5), (3,6), (5,1), (5,2), (5,3), (5,4), (5,5), (5,6) \right\}$$

$$C = \{(1,1), (1,2), (1,3), (1,4), (2,1), (2,2), (2,3), (3,1), (3,2), (4,1)\}$$

$$(i) \quad A' = \left\{ (1,1), (1,2), (1,3), (1,4), (1,5), (1,6), (3,1), (3,2), (3,3), \right. \\ \left. (3,4), (3,5), (3,6), (5,1), (5,2), (5,3), (5,4), (5,5), (5,6) \right\} = B$$

$$(ii) \quad \text{Not } B = B' = \left\{ (2,1), (2,2), (2,3), (2,4), (2,5), (2,6), (4,1), (4,2), (4,3), \right. \\ \left. (4,4), (4,5), (4,6), (6,1), (6,2), (6,3), (6,4), (6,5), (6,6) \right\} = A$$



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(iii)

$$A \text{ or } B = A \cup B = \left\{ \begin{array}{l} (1,1), (1,2), (1,3), (1,4), (1,5), (1,6) \\ (2,1), (2,2), (2,3), (2,4), (2,5), (2,6) \\ (3,1), (3,2), (3,3), (3,4), (3,5), (3,6) \\ (4,1), (4,2), (4,3), (4,4), (4,5), (4,6) \\ (5,1), (5,2), (5,3), (5,4), (5,5), (5,6) \\ (6,1), (6,2), (6,3), (6,4), (6,5), (6,6) \end{array} \right\} = S$$

(iv) A and B = $A \cap B = \phi$

(v) A but not C = $A - C$

$$= \left\{ \begin{array}{l} (2,4), (2,5), (2,6), (4,2), (4,3), (4,4), (4,5), \\ (4,6), (6,1), (6,2), (6,3), (6,4), (6,5), (6,6) \end{array} \right\}$$

(vi) B or C = $B \cup C$

$$= \left\{ \begin{array}{l} (1,1), (1,2), (1,3), (1,4), (1,5), (1,6), (2,1), (2,2), \\ (2,3), (3,1), (3,2), (3,3), (3,4), (3,5), (3,6), \\ (4,1), (5,1), (5,2), (5,3), (5,4), (5,5), (5,6) \end{array} \right\}$$

(vii) B and C = $B \cap C = \{(1,1), (1,2), (1,3), (1,4), (3,1), (3,2)\}$

(viii)

$$C' = \left\{ \begin{array}{l} (1,5), (1,6), (2,4), (2,5), (2,6), (3,3), (3,4), (3,5), (3,6), (4,2), \\ (4,3), (4,4), (4,5), (4,6), (5,1), (5,2), (5,3), (5,4), (5,5), (5,6), \\ (6,1), (6,2), (6,3), (6,4), (6,5), (6,6) \end{array} \right\}$$

$$\therefore A \cap B' \cap C' = A \cap A \cap C' = A \cap C'$$

$$= \left\{ \begin{array}{l} (2,4), (2,5), (2,6), (4,2), (4,3), (4,4), (4,5), \\ (4,6), (6,1), (6,2), (6,3), (6,4), (6,5), (6,6) \end{array} \right\}$$



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Question 7:

Two dice are thrown. The events A, B and C are as follows:

A: getting an even number on the first die.

B: getting an odd number on the first die.

C: getting the sum of the numbers on the dice ≤ 5

State true or false: (give reason for your answer)

- (i) A and B are mutually exclusive
- (ii) A and B are mutually exclusive and exhaustive
- (iii) $A = B'$
- (iv) A and C are mutually exclusive are mutually exclusive
- (v) A and B' are mutually exclusive.
- (vi) A', B' and C are mutually exclusive and exhaustive.

Answer 7:

$$A = \left\{ (2,1), (2,2), (2,3), (2,4), (2,5), (2,6), (4,1), (4,2), (4,3), \right. \\ \left. (4,4), (4,5), (4,6), (6,1), (6,2), (6,3), (6,4), (6,5), (6,6) \right\}$$
$$B = \left\{ (1,1), (1,2), (1,3), (1,4), (1,5), (1,6), (3,1), (3,2), (3,3), \right. \\ \left. (3,4), (3,5), (3,6), (5,1), (5,2), (5,3), (5,4), (5,5), (5,6) \right\}$$
$$C = \left\{ (1,1), (1,2), (1,3), (1,4), (2,1), (2,2), (2,3), (3,1), (3,2), (4,1) \right\}$$

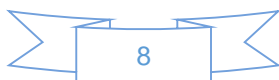
(i) It is observed that $A \cap B = \phi$

\therefore A and B are mutually exclusive.

Thus, the given statement is true.

(ii) It is observed that $A \cap B = \phi$ and $A \cup B = S \therefore$ A and B are mutually exclusive and exhaustive.

Thus, the given statement is true.



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(iii) It is observed that

$$B' = \left\{ (2,1), (2,2), (2,3), (2,4), (2,5), (2,6), (4,1), (4,2), (4,3), \right. \\ \left. (4,4), (4,5), (4,6), (6,1), (6,2), (6,3), (6,4), (6,5), (6,6) \right\} = A$$

Thus, the given statement is true.

(iv) It is observed that $A \cap C = \{(2, 1), (2, 2), (2, 3), (4, 1)\} \neq \emptyset$

\therefore A and C are not mutually exclusive.

Thus, the given statement is false.

(v) $A \cap B' = A \cap A = A$

$\therefore A \cap B' \neq \emptyset$

\therefore A and B' are not mutually exclusive.

Thus, the given statement is false.

(vi) It can be observed that: $A' \cup B' \cup C = S$

However, $B' \cap C = \{(2, 1), (2, 2), (2, 3), (4, 1)\} \neq \emptyset$

Therefore, events A', B' and C are not mutually exclusive and exhaustive.

Thus, the given statement is false.

