

# Mathematics

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(Chapter - 4) (Determinants)

(Class 12)

## Exercise 4.3

### Question 1:

Find area of the triangle with vertices at the point given in each of the following:

(i) (1, 0), (6, 0), (4, 3)

(ii) (2, 7), (1, 1), (10, 8)

(iii) (-2, -3), (3, 2), (-1, -8)

### Answer 1:

$$\text{Area of triangle} = \frac{1}{2} \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix}$$

(i) A(1, 0), B(6, 0), C(4, 3)

$$\text{Area of triangle } ABC = \frac{1}{2} \begin{vmatrix} 1 & 0 & 1 \\ 6 & 0 & 1 \\ 4 & 3 & 1 \end{vmatrix}$$

$$= \frac{1}{2} [1(0 - 3) - 0(6 - 4) + 1(18 - 0)] = \frac{1}{2} (15) = 7.5 \text{ square units}$$

(ii) A(2, 7), B(1, 1), C(10, 8)

$$\text{Area of triangle } ABC = \frac{1}{2} \begin{vmatrix} 2 & 7 & 1 \\ 1 & 1 & 1 \\ 10 & 8 & 1 \end{vmatrix}$$

$$= \frac{1}{2} [2(1 - 8) - 7(1 - 10) + 1(8 - 10)] = \frac{1}{2} (47) = 23.5 \text{ square units}$$

(iii) A(-2, -3), B(3, 2), C(-1, -8)

$$\text{Area of triangle } ABC = \frac{1}{2} \begin{vmatrix} -2 & -3 & 1 \\ 3 & 2 & 1 \\ -1 & -8 & 1 \end{vmatrix}$$

$$= \frac{1}{2} [-2(2 + 8) + 3(3 + 1) + 1(-24 + 2)] = \frac{1}{2} (-30) = -15$$

Area of triangle ABC = 15 square units

### Question 2:

Show that points A(a, b + c), B(b, c + a), C(c, a + b) are collinear.

### Answer 2:

If the points A(a, b + c), B(b, c + a) and C(c, a + b) are collinear, the area of triangle ABC will be zero.

$$\text{Area of triangle } ABC = \frac{1}{2} \begin{vmatrix} a & b + c & 1 \\ b & c + a & 1 \\ c & a + b & 1 \end{vmatrix}$$

$$= \frac{1}{2} \begin{vmatrix} a & a + b + c & 1 \\ b & a + b + c & 1 \\ c & a + b + c & 1 \end{vmatrix} \quad [\text{Applying } C_2 \rightarrow C_1 + C_2]$$

$$= \frac{1}{2} (a + b + c) \begin{vmatrix} a & 1 & 1 \\ b & 1 & 1 \\ c & 1 & 1 \end{vmatrix} \quad [\text{Taking } a + b + c \text{ as common from } C_2]$$

$$= 0 \quad [\because C_1 = C_3]$$

Hence, the points A(a, b + c), B(b, c + a) and C(c, a + b) are collinear.

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## Question 3:

Find values of  $k$  if area of triangle is 4 sq. units and vertices are

(i)  $(k, 0), (4, 0), (0, 2)$

(ii)  $(-2, 0), (0, 4), (0, k)$

### Answer 3:

(i)  $A(k, 0), B(4, 0), C(0, 2)$

$$\begin{aligned} \text{Area of triangle } ABC &= \frac{1}{2} \begin{vmatrix} k & 0 & 1 \\ 4 & 0 & 1 \\ 0 & 2 & 1 \end{vmatrix} \\ &= \frac{1}{2} [k(0 - 2) - 0(4 - 0) + 1(8 - 0)] = \frac{1}{2} (-2k + 8) = -k + 4 \end{aligned}$$

According to question, Area of triangle  $ABC = 4$  square units

$$\text{Therefore, } |-k + 4| = 4 \quad \Rightarrow -k + 4 = \pm 4$$

$$\Rightarrow -k + 4 = 4 \quad \text{or} \quad -k + 4 = -4$$

$$\Rightarrow k = 0 \quad \text{or} \quad k = 8$$

Hence, the value of  $k$  are 0 and 8.

(ii)  $A(-2, 0), B(0, 4), C(0, k)$

$$\begin{aligned} \text{Area of triangle } ABC &= \frac{1}{2} \begin{vmatrix} -2 & 0 & 1 \\ 0 & 4 & 1 \\ 0 & k & 1 \end{vmatrix} \\ &= \frac{1}{2} [-2(4 - k) - 0(0 - 0) + 1(0 - 0)] = \frac{1}{2} (-8 + 2k) = -4 + k \end{aligned}$$

According to question, Area of triangle  $ABC = 4$  square units

$$\text{Therefore, } |-4 + k| = 4 \quad \Rightarrow -4 + k = \pm 4$$

$$\Rightarrow -4 + k = 4 \quad \text{or} \quad -4 + k = -4$$

$$\Rightarrow k = 8 \quad \text{or} \quad k = 0$$

Hence, the value of  $k$  are 0 and 8.

## Question 4:

(i) Find equation of line joining  $(1, 2)$  and  $(3, 6)$  using determinants.

(ii) Find equation of line joining  $(3, 1)$  and  $(9, 3)$  using determinants.

### Answer 4:

(i) Let  $P(x, y)$  be any point lie on the line joining  $A(1, 2)$  and  $B(3, 6)$ . Hence, the points  $A, B$  and  $P$  will be collinear and area of triangle  $ABP$  will be zero.

$$\text{Therefore, Area of triangle } ABP = \frac{1}{2} \begin{vmatrix} 1 & 2 & 1 \\ 3 & 6 & 1 \\ x & y & 1 \end{vmatrix} = 0$$

$$\Rightarrow \frac{1}{2} [1(6 - y) - 2(3 - x) + 1(3y - 6x)] = 0$$

$$\Rightarrow 6 - y - 6 + 2x + 3y - 6x = 0$$

$$\Rightarrow -4x + 2y = 0$$

$$\Rightarrow 2x = y$$

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(ii) Let,  $P(x, y)$  be any point lie on the line joining  $A(3, 1)$  and  $B(9, 3)$ . Hence, the points  $A, B$  and  $P$  will be collinear and area of triangle  $ABP$  will be zero.

$$\text{Therefore, Area of triangle } ABP = \frac{1}{2} \begin{vmatrix} 3 & 1 & 1 \\ 9 & 3 & 1 \\ x & y & 1 \end{vmatrix} = 0$$

$$\Rightarrow \frac{1}{2} [3(3 - y) - 1(9 - x) + 1(9y - 3x)] = 0$$

$$\Rightarrow 9 - 3y - 9 + x + 9y - 3x = 0$$

$$\Rightarrow -2x + 6y = 0$$

$$\Rightarrow x = 3y$$

## Question 5:

If area of triangle is 35 sq. units with vertices  $(2, -6)$ ,  $(5, 4)$  and  $(k, 4)$ . Then  $k$  is

(A) 12                      (B) -2                      (C) -12, -2                      (D) 12, -2

## Answer 5:

$A(2, -6), B(5, 4), C(k, 4)$

$$\text{Area of triangle } ABC = \frac{1}{2} \begin{vmatrix} 2 & -6 & 1 \\ 5 & 4 & 1 \\ k & 4 & 1 \end{vmatrix}$$

$$= \frac{1}{2} [2(4 - 4) + 6(5 - k) + 1(20 - 4k)] = \frac{1}{2} (30 - 6k + 20 - 4k) = 25 - 5k$$

According to question, Area of triangle  $ABC = 35$  square units

$$\text{Therefore, } |25 - 5k| = 35$$

$$\Rightarrow 25 - 5k = \pm 35$$

$$\Rightarrow 25 - 5k = 35 \quad \text{or} \quad 25 - 5k = -35$$

$$\Rightarrow k = \frac{-10}{5} = -2 \quad \text{or} \quad k = \frac{60}{5} = 12$$

Hence, the option (D) is correct.